

# Optimal Design of Minimal Footprint High Frequency Transformer

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**Abstract:** Transformer design procedure may vary essentially in respect of the transformer type and its operating frequency (ranging between 50/60 Hz and a few megahertz). This paper presents a simple and straightforward method based on the optimal choice of core geometry of a high frequency transformer (HFT) used in Solid State Transformer (SST) applications. The core of SST is the HFT which largely influences its size and overall performance. The proposed design procedure for HFT focuses on optimizing the core geometry coefficient (in  $\text{cm}^5$ ) with a constraint inflicted on loss density. The core geometry coefficient has direct impact on the regulation and copper loss and the procedure results in a robust overall design with minimal footprint. Also, the procedure intends to bring all the operating parameters like regulation, losses and temperature rise within permissible limits while retaining desired efficiency. Thus an energy-efficient design is achieved with minimal footprint. The optimization procedure is implemented using recently developed Moth-flame Optimization (MFO) algorithm. The results of the MFO algorithm are compared with the well-established PSO technique. An experimental prototype is built to validate the findings.

**Keywords:** Optimization, Medium Frequency transformer, Bio-inspired algorithm, Solid State Transformer, Isolated DC-DC Converter.

## 1 Introduction

In the global pursuit for accomplishing green environment, research efforts are motivated to modernize major components of the electric utility system. One such effort is the development of Solid State Transformer as a potential alternative to conventional distribution transformer (CDT). Unlike CDT, SST is pollution-free and hence considered as a milestone invention to meet the needs of sustainable energy future. SST has been drawing huge attention as prospective component of utility distribution systems in recent years, thanks to its embedded intelligence and ability to provide additional services besides energy transformation and isolation.

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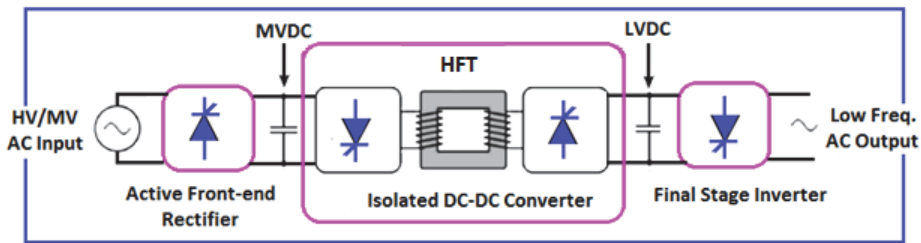


Fig. 1 – Typical Three-stage SST architecture.

The nucleus of the three-stage SST system shown in Fig. 1 is the medium frequency isolated dc-dc converter which serves as an interface between medium voltage ac and low voltage ac/dc grids [1 – 3]. The converter and hence the high frequency transformer (HFT) design greatly influences the performance as well as footprint of the SST. Operation at high/medium frequencies though results in high power densities and reduced size and weight for the HFT, it also leads to increased core loss, magnetic saturation and temperature rise at high voltages [4]. Therefore choice of magnetic material becomes crucial to attain high power densities and efficiencies. Significant attention must be paid to issues related to thermal management as well, in order to overcome the increased loss density with reduced footprint. Further, wire selection must be carefully done because skin and proximity effects in the windings become more pronounced at high frequencies. Thus a cumulative design approach is needed for HFT such that all the challenges concerned with high frequency operation are overcome simultaneously offering desired efficiency and regulation.

## 2 Literature Background

Many approaches to high/medium frequency transformer (HFT/MFT) design for various applications were reported in the past. Previously, HFT design for switching power supplies were developed [5 – 8]. Later, efforts were made to design HFT with minimal size and weight for high power isolated DC-DC converters employed in distribution grids. This was deemed appropriate for offshore wind installations as reported in [4] where a 500 Hz transformer was shown to be 1/3rd the weight of its equivalent 50 Hz one. The prospects of deploying HFTs in traction applications were also discussed in the past [9]. A 350 kW/8kHz transformer as a substitute for a 16.7 Hz transformer was designed for on-board railway vehicles [10] and was proved to have a significant volume reduction. Recently, attempts on design of high/medium frequency transformers for SST applications have been widely reported [11 – 14]. All the aforementioned research endeavours have focused chiefly on the benefits of utilizing higher frequencies, rather than on the design aspects and optimization of

such a transformer. A new procedure based on brute-force approach for design optimization of MFT for SST applications has been documented in [15]. While the procedure seems really interesting, the generation of all feasible solutions is really cumbersome and the data processing is time consuming.

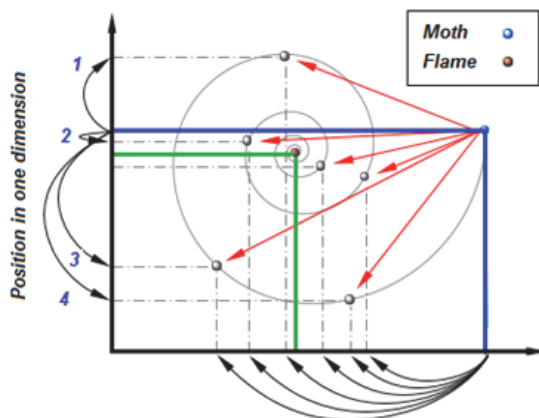
Further scrutiny of literature divulges information on research efforts undertaken to optimize the HFT design. Typical attempts on optimization concentrated on a factor named area product by which the amount of power handled by the core is established [6, 16]. Nevertheless, the proposed procedure has not been validated for high power, high frequency applications. A design optimization of HFT with high isolation requirements and thermal management based on round litz wires [17] has been discussed in [18]. Also, optimization with emphasis on thermal and insulation design [19] and maximizing the power density by accounting for tuned leakage inductance [20, 21] were documented in the past. A HFT optimization design to exploit the utilization of the transformer to achieve high power density with minimum transformer loss has been reported in [22]. Recently, a medium frequency transformer design has been proposed based on open-source optimization framework where the magnetic field calculation is done by a built-in FEM solver [23, 24].

Thus, several of the challenges pertaining to HFT/MFT design mentioned earlier have been addressed individually and solutions provided in the past by researchers across the globe. However, a comprehensive design taking into account all the significant challenges are rarely not yet documented in literature. Therefore, further investigations are needed in order to achieve high power density, better regulation along with good thermal management while retaining high efficiency for the HFT. Additionally, all the recorded research work have centered around either single or multi-objective optimization with or without constraints along with a method to check limits on operating parameters prior to arriving at an optimal solution to the problem. This is a lengthy process because whenever an operating parameter violates the bounds, the algorithm hunts for a new optimal solution that satisfies the limits.

With all the above concerns in mind, the work reported in [25] was intended to develop a novel optimization procedure for the design of HFT which takes into account the core geometry coefficient (in  $\text{cm}^5$ ) [6] with a constraint inflicted on loss density. The method proposed confines all the working parameters within expected limits while preserving desired efficiency. Further, the method resulted in a minimal footprint for the HFT. However, a laboratory prototype of the HFT was not developed to support the claims. This paper on the other hand validates the findings by constructing a laboratory prototype of the converter with the HFT before and after optimization. The efficiency of the converter with HFT before and after optimization were also compared for better understanding.

### 3 MFO Algorithm

Bio-inspired optimization algorithms are finding extensive applications in solving real and composite engineering design problems over the past few years [26, 27]. Significant attention is being given to these algorithms owing to complex and dynamic nature of the problems, wide range of possible multidimensional solutions, and challenges related to partial and/or limited information for arriving at an optimal solution [28, 29]. Adequate literature is available in this domain with major focus on Genetic Algorithms (GA), Ant Colony Optimization (ACO) and Particle Swarm Optimization (PSO). However, in recent times, number of new algorithms are developed mimicking the behaviour of bio-organisms, namely, Whale Optimization algorithm (WOA), Dragon Fly (DA) algorithm, Ant-Lion Optimization (ALO), Grey-Wolf Optimizer (GWO) and so on. One such algorithm is the Moth-Flame Optimization (MFO) algorithm proposed in [30]. The MFO algorithm is developed based on the tendency of moths to adopt transverse orientation for their navigation towards moonlight. However they are diverted by artificial lights and end up following deadly spiral paths. This activity of moths is mathematically modeled for optimization as shown in Fig. 2.



**Fig. 2** – *Mathematical modeling of MFO algorithm* [31].

This paper is aimed at using the MFO algorithm for high frequency transformer (HFT) design problem. Initially, optimization problems with respect to transformer design have been solved using GA [8, 31]. Later, Bacterial Foraging Algorithm (BFA) [32] and PSO algorithm [33] have been applied to solve these problems. In this paper, recently developed MFO algorithm which has not been applied to transformer design problem hitherto, is adopted to solve the design problem of HFT used in Solid State Transformer (SST) applications. The results are then compared with the well established PSO technique. The

proposed method for optimization is more simple and uncomplicated in comparison to the methods documented in literature. The optimal HFT is then implemented as a laboratory prototype for low power applications using isolated half-bridge converter.

#### 4 Optimization Procedure for HFT

The step-by-step design procedure for HFT design of dc-dc converters outlined by McLyman [6] has been followed here. An isolated half-bridge converter is chosen for the design case study and the corresponding design equations are presented along with the procedure for optimization. The design inputs to the optimization problem are the power rating  $P_o$  of the isolated half-bridge converter and the input and output voltages,  $U_{in}$  and  $U_o$  respectively. Efficiency ( $\eta$ ), % regulation ( $\alpha$ ), utilization factor ( $k_u$ ) and waveform coefficient ( $K_w$ ) are kept fixed. The design of HFT is normally realized for a given temperature rise. However, the design can be realized for a known % regulation,  $\alpha$ . The  $\alpha$ , as defined by McLyman is related to two coefficients namely, the electrical coefficient,  $K_{el}$  and the core geometry coefficient,  $K_{cg}$  given by

$$K_{el} = 0.145k_w^2 f_s^2 B^2 10^{-4}, \quad (1)$$

$$K_{cg} = \frac{S}{2K_{el}\alpha}, \quad (2)$$

where  $S$  is the total apparent power in watts,  $f_s$  is the operating frequency in Hz and  $B$  is the flux density in Tesla.  $K_{cg}$  can also be expressed as

$$K_g = \frac{A_w A_e^2 k_u}{L_{mt}} [\text{cm}^5], \quad (3)$$

where  $A_w$  is the window area in  $\text{cm}^2$ ,  $A_e$  is the effective core cross-section in  $\text{cm}^2$  and  $L_{mt}$  is the mean length of the turn in cm. It is clear from (2) and (3) that  $K_{cg}$  affects the regulation and copper loss besides influencing the size of the magnetic components. Thus  $K_{cg}$  can be optimized to design a highly compact and efficient HFT, concurrently confining the other key design requirements like % regulation, current density in the windings, copper losses, temperature rise etc., within specified bounds.

For a given % regulation,  $K_{cg}$  is a function of two variables namely,  $f_s$  and  $B$  as noted from (1) and (2). The variation of core geometry coefficient with operating frequency and flux density is depicted in Fig. 3. In low frequency transformer design, with emf induced per turn remaining constant, increasing the operating frequency of the transformer actually reduces the peak flux density of the core and vice-versa. However the proposed design for HFT does not

necessitate constant emf/turn and hence flux density and frequency are chosen as free parameters to establish optimal core geometry.

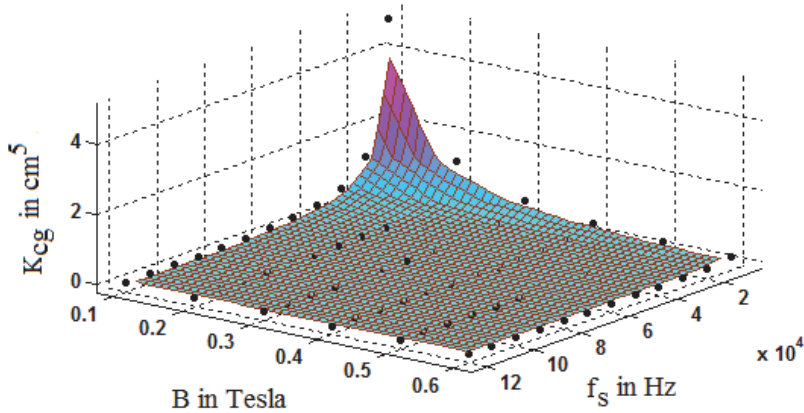


Fig. 3 – Plot of coefficient of core geometry vs operating frequency and flux density.

With frequency and flux density as free parameters and a constraint inflicted on specific loss, the objective function of the design optimization problem is given by:

**Minimize  $K_{cg}$  such that**

(i)  $f_{s\min} < f_s < f_{s\max}$

(ii)  $B_{\min} < B < B_{\max}$

**with the constraint**  $W_{sp}(f_s, B) - 0.05 \times P_s < 0^\#$

where  $W_{sp}$  is the specific loss in W/kg and  $P_s = P_o(1/\eta + 1)$  is the total apparent power in W.

**# Specific loss is assumed to be limited to 5% of total apparent power.**

In the proposed optimization procedure, instead of holding  $V/f$  constant to eliminate over-fluxing as in the case of low frequency transformer, the operating frequency is swung across a given range together with flux density. This is because the choice of core and its dimensions are made only after seeking an optimum solution for  $K_{cg}$ .

With the best generated free parameters and the optimal value for core geometry coefficient obtained from the MFO algorithm, the appropriate choice of core material is made from the core data table corresponding to the optimal value. Generally, the core with a little higher value for  $K_{cg}$  than the optimal value is chosen to ascertain minimal copper loss. The dimensions of the selected core viz., mean length of the turn ( $L_{mt}$ ), magnetic path length ( $L_{mp}$ ), total weight of the core ( $W_{fe}$ ), total copper weight ( $W_{cu}$ ), minimum cross-sectional area of the core

( $A_c$ ), window area ( $A_w$ ), area product ( $A_p$ ) and overall surface area of the magnetic component ( $A_s$ ) are extracted from the core data table. With these dimensions, the performance parameters of the HFT are estimated.

The number of primary turns is obtained by

$$N_{pri} = \frac{U_{pri} 10^4}{K_w B_{opt} f_{s\_opt} A_c}, \quad (4)$$

where  $B_{opt}$  and  $f_{s\_opt}$  are the best fit values for flux density in Tesla and frequency in Hertz respectively and

$$U_{pri} = \frac{U_{in}}{2} (2D_{max}) - I_{pri} R_q \quad (5)$$

is the average primary voltage in volts,  $D_{max}$  is the maximum duty cycle of the converter and  $R_q$  is the transistor resistance in ohms.

The average primary current for the half-bridge converter is given by

$$I_{pri} = \frac{2P_o}{U_{in} \eta}. \quad (6)$$

The current density in the windings in amps/cm<sup>2</sup> is then calculated by

$$J = \frac{P_s 10^4}{K_w K_u B_{opt} f_{s\_opt} A_p}, \quad (7)$$

where  $P_s$  is the total apparent power in watts and  $A_p$  is the area product in cm<sup>2</sup>.

With the known value of current density, the primary wire area in cm<sup>2</sup> is estimated as

$$A_{wpri} = \frac{I_{pri}}{J \sqrt{2D_{max}}}. \quad (8)$$

A proper choice of wire is made from the wire table with the required wire area. If the wire area from the table is in excess of 10% of the required wire area, then the next smallest size is chosen.

Upon selecting appropriate wire for the design, the primary winding resistance and hence primary copper losses are estimated. The primary winding resistance in ohms,

$$R_{pri} = L_{mt} (N_{pri}) \left( \frac{\mu\Omega}{\text{cm}} \right) 10^{-6}, \quad (9)$$

where  $\mu\Omega/\text{cm}$  is the specific resistance of the chosen wire. The primary copper losses in watts are given by

$$P_{cup} = \frac{I_{pri}^2}{2D_{max}} R_{pri} . \quad (10)$$

The number of secondary turns on each side of the centre tap (if any) is then calculated using the equation below:

$$N_{sy} = \frac{N_{pri} (U_o + U_d)}{U_{pri}} \left( 1 + \frac{\alpha}{100} \right), \quad (11)$$

where  $U_d$  is the diode voltage drop. Similar to the primary winding design, the secondary wire area ( $A_{wsy}$ ), secondary winding resistance ( $R_{sy}$ ) and hence secondary copper losses ( $P_{cus}$ ) are estimated. The new value of window utilization factor is then updated as

$$K_{unew} = \frac{N_{pri} S_n A_{wire\_p} + N_{sy} S_n A_{wire\_s}}{A_w}, \quad (12)$$

where  $A_{wire\_p}$  and  $A_{wire\_s}$  are the selected wire areas from the wire table for the primary and secondary windings respectively.  $S_n$  represents the number of strands of primary and secondary wires given by the ratio of actual wire area to the bare wire area obtained from the wire table. Following  $K_u$ , the % regulation  $\alpha$  is also updated with the new value

$$\alpha_{new} = \frac{P_{cu}}{P_o} 100, \quad (13)$$

where  $P_{cu}$  is the sum of primary and secondary copper losses. The new value of flux density is now calculated as

$$B_{new} = \frac{U_{pri} 10^4}{K_w f_{s\_opt} A_c N_{pri}} \quad (14)$$

and the corresponding loss density is given by

$$W_{sp} = 3.18 \times 10^{-4} (f_{s\_opt})^{1.51} (B_{new})^{2.747}. \quad (15)$$

Subsequently, the core losses in watts are estimated to be

$$P_{fe} = W_{sp} (W_{fe}) 10^{-3}. \quad (16)$$

The final stage of the design includes computation of loss density ( $W/cm^2$ ) and the resultant temperature rise in  $^{\circ}C$ .

$$\lambda = \frac{P_{tot}}{A_s}, \quad (17)$$

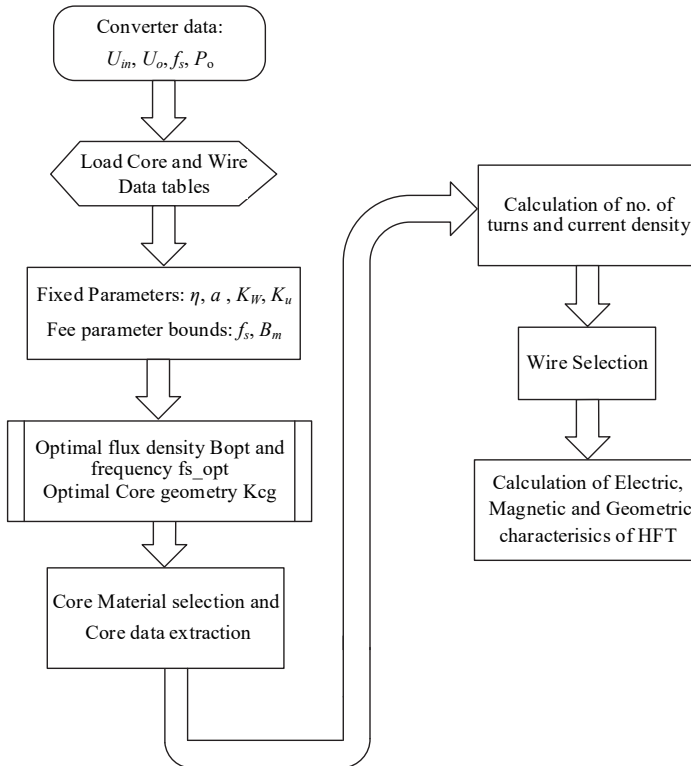
where  $P_{tot}$  is the sum of core and copper losses. The temperature rise is given by

$$\Delta T = 450(\lambda)^{0.826}. \quad (18)$$



## 5 Optimization Results and Discussion

The optimization procedure and the parameter calculation for HFT described in the previous section are presented as a simple flow diagram in Fig. 4. A single dc-dc converter module is considered for evaluating the case study whose specifications are listed in **Table 1**. For SST applications, several such modules can be connected in parallel at the low voltage side (LVDC link) and in series at the high/medium voltage side (HVDC/MVDC link) as per requirement as shown in Fig. 5. The fixed parameters assumed for the case study under consideration is presented in **Table 2**.



**Fig. 4** – Flowchart for HFT optimization.

**Table 1**

*Design specifications of a single converter module.*

Design Parameters	Specification
Output Power, $P_o$ (W)	250
Nominal Input Voltage, $U_{in}$ (V)	100
Output Voltage, $U_o$ (V)	75
Output Current, $I_o$ (A)	3.33

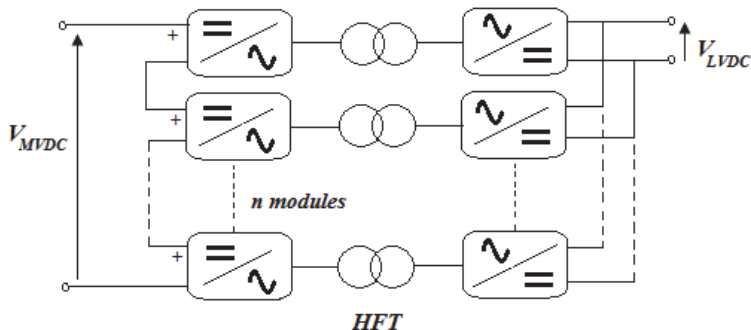


Fig. 5 – Modular arrangement of isolated DC-DC converters.

**Table 2**  
Fixed parameters for optimization.

% Efficiency, $\eta$	96
% Regulation, $\alpha$	0.6
Window utilization factor, $K_u$	0.4
Waveform coefficient, $K_w$ (for square wave)	4.0

The free parameters, namely,  $f_s$  and  $B$  are varied over a wide range within expected limits to find the best optimal value for  $K_{CG}$ . The operating frequency is varied between 10 kHz and 75 kHz and the maximum flux density between 0.1 T and 0.6 T. The saturation flux density of the material employed for the core is taken as the upper limit. However, 10 – 20% margin of safety is allowed to keep away from saturation. As ferrite core is chosen for the design case study, the upper limit for  $B$  is fixed at 0.6 T. The choice of ferrite core can be attributed to the fact that they exhibit lower core losses ( $> 20$  kHz) and are available in an assortment of geometric shapes.

In the direct design procedure for HFT, the choice of 15 kHz for frequency and 0.45T for the corresponding flux density is arbitrary. The core geometry corresponding to the chosen values of frequency and flux density is obtained as  $0.05164 \text{ cm}^5$ . After optimization using MFO, the best values for free parameters are established as 50 kHz and 0.1609 T and the optimal core geometry is  $0.03635 \text{ cm}^5$ . A relative comparison of the performance of HFT before and after optimization is presented in **Tables 3** and **4**. The core data for the calculated value of  $K_g$  before optimization and that for the optimal value of  $K_g$  are listed in **Table 3**. The look up table for the core data is generated with the details obtained from Magnetics®, the leading magnetic component suppliers. F-type ferrite material has been chosen as they are very much suitable for converter transformers with

reasonably good permeability, low losses and high saturation. **Table 4** presents the electric, magnetic and geometric characteristics of the HFT before and after optimization.

**Table 3**  
*Core data before and after optimization.*

Core data	Before optimization	After optimization	Core data	Before optimization	After optimization
$K_{cg}$ (cm <sup>5</sup> )	0.05164	0.03635	$W_{cu}$ (gm)	36.39	19.96
Core material part No.	EE 37	EE 44	$A_c$ (cm <sup>2</sup> )	0.821	1.01
$L_{mp}$ (cm)	6.94	5.19	$A_w$ (cm <sup>2</sup> )	1.5396	0.7226
$L_{mt}$ (cm)	6.646	7.77	$A_p$ (cm <sup>4</sup> )	1.264	0.7298
$W_{je}$ (gm)	33.09	26	$A_s$ (cm <sup>2</sup> )	45.39	41.34

**Table 4**  
*Electric, magnetic and geometric characteristics of HFT before and after optimization.*

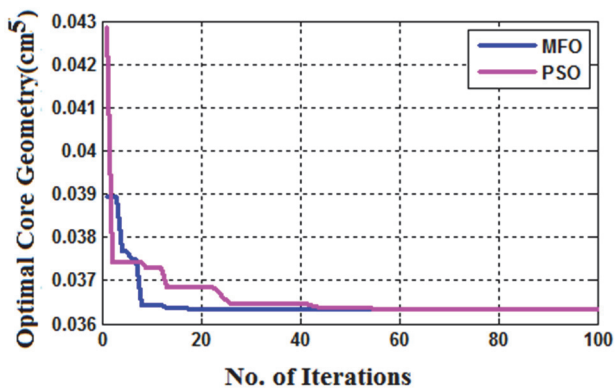
Transformer characteristics	Before optimization	After optimization	Transformer characteristics	Before optimization	After optimization
$J$ (A/cm <sup>2</sup> )	383.86	557.81	$B_{new}$ (T)	0.4482	0.1632
$R_{pri}$ ( $\Omega$ )	0.0292	0.0672	$N_{pri}$	21	13
$R_{sy}$ ( $\Omega$ )	0.0487	0.119	$N_{sy}$	35	23
$P_{cu}$ (W)	0.7569	1.857	$A_{wpri}$ (cm <sup>2</sup> )	0.007	0.005
$P_{je}$ (W)	2.347	0.7084	$A_{wsy}$ (cm <sup>2</sup> )	0.006	0.004
$P_{tot}$ (W)	3.104	2.565	$S_n$	1	2
$\lambda$ (W/cm <sup>2</sup> )	0.06834	0.0621	$W_{sp}$ (W/kg)	70.93	27.25
$\alpha_{new}$ (%)	0.2949	0.7234	$\Delta T$ ( $^{\circ}$ C)	49.078	45.29

It is inferred from **Table 3** that optimizing the core geometry results in reduction of both core and copper weights. Though an increase in core cross-sectional area is observed, the window area is very much reduced and hence the area product. Thus a minimal footprint is achieved for HFT. Analyzing the data presented in **Table 4**, it is understood that despite an increase in copper losses, the total losses are reduced roughly by 20% following optimization. The specific loss is limited to 5% of the total apparent power as per the problem statement. The new value of regulation is 0.72% which is well within desired limits. Also, the temperature rise is limited to 45 $^{\circ}$ C after optimization. This proves the effectiveness of the proposed optimization procedure.

**Table 5**  
*Comparison of Performance of MFO and PSO algorithms.*

Optimization algorithm	Operating frequency, $f_{s\_best}$ (kHz)	Maximum flux density, $B_{best}$ (T)	Coefficient of core geometry, $K_{cg\_opt}$ (cm <sup>5</sup> )	Average overall computational time (s)	Average no. of iterations for convergence
<b>MFO</b>	50	0.1609	0.03635	0.7939	23
<b>PSO</b>	49.88	0.1611	0.03642	0.4039	66.6

A comparative evaluation of the MFO algorithm with the PSO technique is made and the results presented in **Table 5**. The comparison is carried out for the test case presented in **Table 1**. Both the algorithms are compared based on identical search agents (equal to 100). The convergence speed and the number of iterations required for convergence are averaged over 10 successive runs. For the proposed optimization problem, it is discerned from the table that both the algorithms return identical optimal solution though they differ in speed of computation, consistency in producing solutions in consecutive runs and convergence.



**Fig. 6** – Plot of convergence for MFO and PSO algorithms.

Fig. 6 shows the convergence of the MFO and PSO algorithms plotted for case study under consideration. It is clear from the plot that MFO converges quickly than PSO. However, it is observed from **Table 5** that though MFO is quick to converge compared to PSO algorithm, the relative computational time is the least with PSO. This is because the computational time per iteration is the least with the PSO algorithm. Additionally, MFO is found to be more consistent in producing the optimal solution than PSO.

## 6 Experimental Validation and Results

The proposed optimization procedure for HFT discussed in the preceding sections is validated with an experimental setup. The HFTs before and after optimization are tested for their performance by incorporating them into the Half-bridge converter circuit and the results are compared to highlight the benefits of the proposed optimization procedure. Since the key objective here is the design optimization of HFT, a simple half-bridge dc-dc converter topology is chosen for unidirectional and Modular SST applications. Nevertheless, the design optimization can be carried out with any dc-dc converter topology that is deemed appropriate for a specific application.

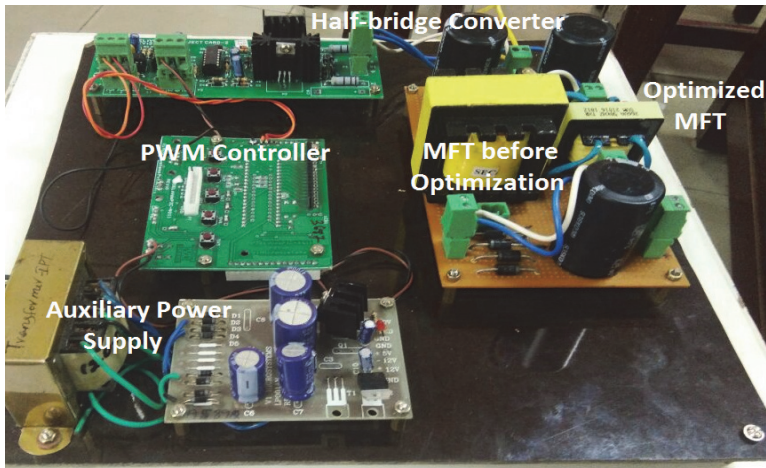
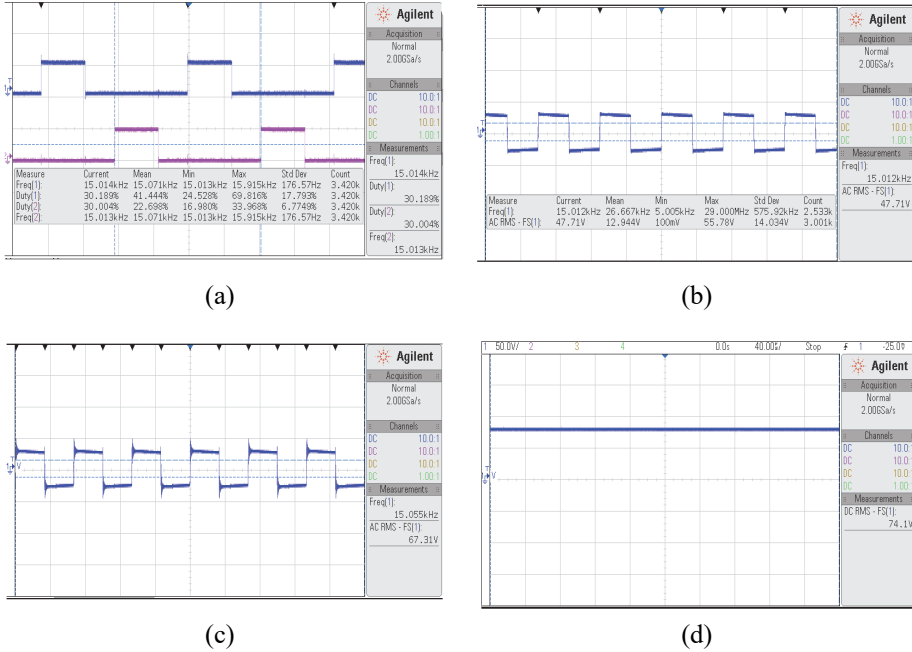


Fig. 7 – Experimental prototype of Half- bridge converter with HFT.

**Table 6**  
*Ratings of major components of the prototype.*

Component	Part No.	Ratings
MOSFET	IRFP840	500V, 8A, 0.85Ω
Diode	MUR 440	400V, 4A
Capacitors	-	330μF, 450V
Optocoupler IC	A4506	-
MOSFET Driver	IRS2110	500V dc offset, 10-20V o/p, 130ns & 120ns $t_{on/off}$
PWM Controller	dsPIC30F4011	16 bit controller with 6 PWM output channels
Resistive Load	-	25Ω
HFT1	EE375	Turn's ratio: 1.4, 15 kHz
HFT2	EE44008	Turn's ratio: 1.4, 50 kHz

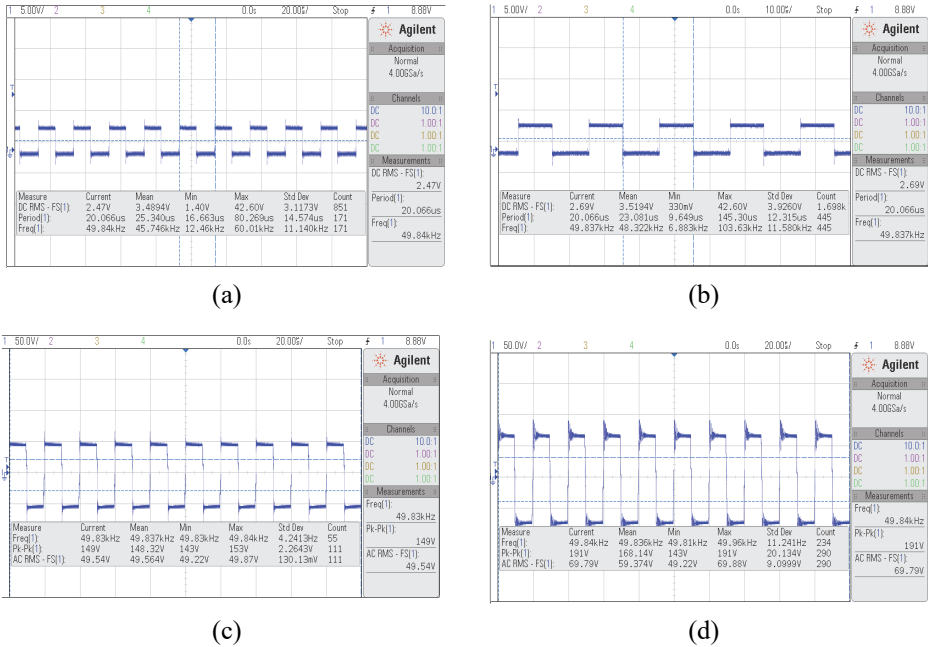
A single 250 W Half-bridge converter circuit is built with provisions for plugging in the HFTs before and after optimization as shown in Fig. 7. A 100 V dc input is fed to the converter through bridge rectifier module and the results are recorded by plugging in the HFTs one after the other. The ratings of major components are presented in **Table 6**. The results obtained are presented below in Figs. 8 – 10.



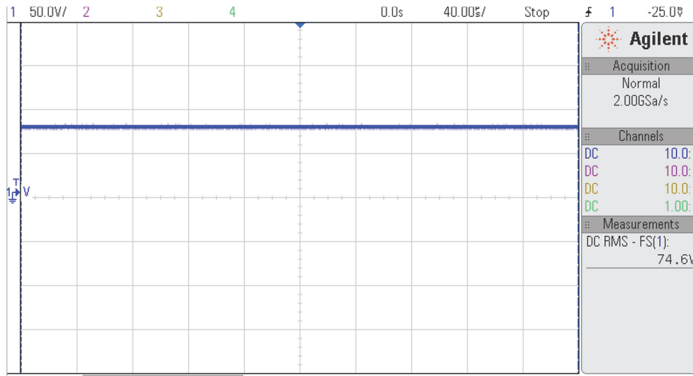
**Fig. 8** – Results from Prototype with HFT before Optimization (a) PWM pulses to the MOSFETs (b) Primary voltage of HFT (c) Secondary voltage of HFT (d) Output voltage of the converter.

Fig. 8 depicts the performance of Half-bridge converter with HFT before optimization. The operating frequency of the HFT is 15 kHz. The primary and secondary voltages of the HFT are observed to be 47.71 V and 67.31 V respectively. The converter output voltage is 74.1 V. The dc current drawn at the source is measured to be 2.4 A. The performance of Half bridge converter with HFT after optimization is illustrated in Figs. 9 and 10. The HFT operates at 50 kHz and the primary and secondary voltages are found to be 49.54 V and 69.79 V respectively. The converter output voltage is found to be 74.6 V and input dc current is measured to be 2.35 A. The efficiencies of the converter with the HFT before and after optimization are presented in **Table 7**.

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**Fig. 9 – Results from Prototype with HFT after Optimization**  
 (a) PWM pulses to the MOSFET1 (b) PWM pulses to the MOSFET2  
 (c) Primary voltage of HFT (d) Secondary voltage of HFT.



**Fig. 10 – Output Voltage of the Converter after Optimization.**

**Table 7**  
*Efficiency of Half-bridge Converter.*

Half-Bridge Converter with HFT	% Efficiency
Before Optimization	91.50
After Optimization	94.73

It is observed that the converter with the optimized HFT produces better results for the given specifications even with a reduced footprint. This proves the effectiveness of the proposed optimization procedure.

## **7 Conclusion**

A simple and robust single-objective design optimization procedure for HFTs employed in modular SST applications was described in this paper. The key purpose was to optimize the core geometry coefficient with a constraint imposed on specific loss in such a way that the design procedure yields a more compact and efficient HFT with all operating parameters under desirable limits. MFO algorithm was applied to solve the proposed optimization problem and its performance was compared with the well-established PSO algorithm. It was inferred that MFO exhibited relatively high speed of convergence whereas PSO required relatively low computational time. An experimental prototype of Half-bridge converter has been developed with the designed HFT and the results established the success of the proposed optimization procedure.

## **8 Acknowledgment**

This work was supported by the All India Council for Technical Education (AICTE) [File No. 828/RIFD/RPS/POLICY-1/2016-17 dated 2<sup>nd</sup> August 2017].

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